

PROBLEM 2 (32 PTS)

- In ALL these problems (a, b, c), you MUST show your conversion procedure. **No procedure = zero points.**
- a) Convert the following decimal numbers to their 2's complement representations: binary and hexadecimal. (12 pts)
 - ✓ 101.3125, -64.6875, -31.65625.

- b) Complete the following table. The decimal numbers are unsigned: (6 pts)

Decimal	BCD	Binary	Reflective Gray Code
278		10101011	10110101
		10111010	110001101
	100101010111		

- c) Complete the following table. Use the fewest number of bits in each case: (14 pts)

REPRESENTATION			
Decimal	Sign-and-magnitude	1's complement	2's complement
-257		10111111	10000000
	1100111	010010001	
-128			10000011

PROBLEM 3 (30 PTS)

- a) Perform the following additions and subtractions of the following unsigned integers. Use the fewest number of bits n to represent both operators. Indicate every carry (or borrow) from c_0 to c_n (or b_0 to b_n). For the addition, determine whether there is an overflow. For the subtraction, determine whether we need to keep borrowing from a higher bit. (8 pts)

Example ($n=8$):

✓ $54 + 210$

$$\begin{array}{r}
 \overset{c_8}{1} \quad \overset{c_7}{0} \quad \overset{c_6}{0} \quad \overset{c_5}{0} \quad \overset{c_4}{0} \quad \overset{c_3}{0} \quad \overset{c_2}{0} \quad \overset{c_1}{0} \quad \overset{c_0}{0} \\
 54 = 0x36 = 00110110 + \\
 210 = 0xD2 = 11010010 \\
 \hline
 \text{Overflow!} \rightarrow 100001000
 \end{array}$$

✓ $77 - 194$

$$\begin{array}{r}
 \text{Borrow out!} \rightarrow b_8=1 \quad b_7=0 \quad b_6=0 \quad b_5=0 \quad b_4=0 \quad b_3=1 \quad b_2=0 \quad b_1=0 \quad b_0=0 \\
 77 = 0x4D = 01001101 - \\
 194 = 0xC2 = 11000010 \\
 \hline
 00001011
 \end{array}$$

- ✓ $173 + 75$
- ✓ $69 + 211$

- ✓ $87 - 256$
- ✓ $241 - 37$

- b) We need to perform the following operations, where numbers are represented in 2's complement: (16 pts)

- ✓ $-87 + 256$
- ✓ $490 + 22$
- ✓ $-35 + 65$
- ✓ $-255 - 230$

- For each case:
 - ✓ Determine the minimum number of bits required to represent both summands. You might need to sign-extend one of the summands, since for proper summation, both summands must have the same number of bits.
 - ✓ Perform the binary addition in 2's complement arithmetic. The result must have the same number of bits as the summands.
 - ✓ Determine whether there is overflow by:
 - i. Using c_n, c_{n-1} (carries).
 - ii. Performing the operation in the decimal system and checking whether the result is within the allowed range for n bits, where n is the minimum number of bits for the summands.
 - ✓ If we want to avoid overflow, what is the minimum number of bits required to represent both the summands and the result?

- c) Get the multiplication results of the following numbers that are represented in 2's complement arithmetic with 4 bits. (6 pts)

✓ $0111 \times 0110, 1100 \times 0101, 1011 \times 1010.$

